#### EC933-G-AU – Lecture 2 26 October 2005

#### Macroeconomic Theories of Balance of Payments Adjustment: Flow Approaches

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#### Plan of talk

#### • introduction

- 1. BoP adjustment through exchange-rate variation: the (critical) elasticity approach
- 2. BoP adjustment through income variation: the (foreign trade) multiplier approach
- 3. an integrated approach to BoP adjustment: Laursen-Metzler (1950) model
- 4. Mundell (1960-1964) Fleming (1962) model

• wrap-up

#### Aim and learning outcomes

- **aim:** understand and interpret the flow approaches to BoP adjustment
- learning outcomes
  - distinguish the elasticity vs the multiplier approach to BoP
  - derive and interpret
    - the Marshall-Lerner critical elasticity condition
    - the transfer problem (in diffirent model contexts)
    - the Laursen-Metzler (1950) model integrating the elasticity and multiplier approaches
  - derive and analyse the policy implications of the Mundell (1960-1964) –
     Fleming (1962) static model

#### Elasticity approach: assumptions

• **BoP**  $\equiv$  NX  $\approx$  CA

(abstracting from NFI, current transfers; and capital movements)

- simple model
  - 2 countries, 2 goods with fixed prices in national currency ⇔ traditional producer's (seller's/exporter's) currency pricing, PCP
  - each good available only in one of the countries (endowment differences)
     => relative price b/n home and foreign good coincides with ToT

$$q^{ToT} \equiv \frac{P_{EX}}{SP_{IM}^*}$$

- trade in a **not perfectly homogeneous** good
  - H and F good similar, so that substitution in consumption possible
  - but *differentiated*, distinctive to consumers according to origin (*H* or *F*)

#### Elasticity approach: BoP adjustment

#### 1. a change in NER, S

- 2. causes directly a **change in relative price** of goods, given in this simple model by **ToT**,  $q^{ToT}$
- 3. which induces further a **change in the quantities demanded** for the two goods,  $q_{EX}^D$  and  $q_{IM}^D$
- 4. and, under the assumption of **perfectly elastic** (geometrically, horizontal) **supply** (curve), implicit in the simpler model version,  $q_{EX}^D \equiv q_{EX}^S \equiv q_{EX}$  and  $q_{IM}^D \equiv q_{IM}^S \equiv q_{IM}$
- 5. BoP disequilibrium (goods and services) will **adjust**

### Elasticity approach: policies, definitions

- BoP adjustment: automatic or policies, Johnson (1958)
   expenditure switching: NER => ToT => switch expenditure
  - expenditure **reducing**: if trade deficit, fiscal and/or monetary restriction to *reduce* total expenditure, hence that on imports
- BoP measured in **value** = **price** x **quantity** 
  - export quantities vary in same direction as NER (=> price)
  - *import* quantities vary in *opposite* direction to NER (=> price)
  - *overall* effect on BoP not clear from "directional" analysis
- elasticities of exports and imports w.r.t. NER

$$\eta_{EX} \equiv \frac{\frac{\Delta q_{EX}}{q_{EX}}}{\frac{\Delta S}{S}} \equiv \frac{\Delta q_{EX}}{\Delta S} \frac{S}{q_{EX}}, \qquad \eta_{IM} \equiv -\frac{\frac{\Delta q_{IM}}{q_{IM}}}{\frac{\Delta S}{S}} \equiv -\frac{\Delta q_{IM}}{\Delta S} \frac{S}{q_{IM}}$$

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Elasticity approach:  
deriving the Marshall-Lerner condition  

$$CA = P_{EX}q_{EX} - SP_{IM}^{*}q_{IM}$$

$$CA + \Delta CA = P_{EX}(q_{EX} + \Delta q_{EX}) - (S + \Delta S)P_{IM}^{*}(q_{IM} + \Delta q_{IM})$$

$$\Delta CA = P_{EX}\Delta q_{EX} - SP_{IM}^{*}\Delta q_{IM} - \Delta SP_{IM}^{*}q_{IM} - \Delta SP_{IM}^{*}\Delta q_{IM}$$

$$\Delta CA \approx P_{EX}\Delta q_{EX} - SP_{IM}^{*}\Delta q_{IM} - \Delta SP_{IM}^{*}q_{IM} - \Delta SP_{IM}^{*}\Delta q_{IM}$$

$$\Delta CA \approx P_{EX}\Delta q_{EX} - SP_{IM}^{*}\Delta q_{IM} - \Delta SP_{IM}^{*}q_{IM} =$$

$$= \Delta SP_{IM}^{*}q_{IM} \left(\frac{P_{EX}\Delta q_{EX}}{\Delta SP_{IM}^{*}q_{IM}} - \frac{SP_{IM}^{*}\Delta q_{IM}}{\Delta SP_{IM}^{*}q_{IM}} - 1\right) =$$

$$= \Delta SP_{IM}^{*}q_{IM} \left(\frac{\Delta q_{EX}}{\Delta S} - \frac{S}{q_{EX}}}{q_{EX}} - \frac{q_{EX}}{S} - \frac{P_{EX}}{P_{IM}^{*}q_{IM}}}{q_{IM}} - 1 - \frac{\Delta q_{IM}}{\Delta S} - \frac{S}{q_{IM}}}{q_{IM}}\right) =$$

$$= \Delta SP_{IM}^{*}q_{IM} \left(\eta_{EX} - \frac{P_{EX}q_{EX}}{SP_{IM}^{*}q_{IM}}}{q_{IM}} - 1 + \eta_{IM}\right) - \eta_{EX} + \eta_{IM} > 1$$

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# Elasticity approach: elasticity pessimism, elasticity optimism, forex market stability

• Marshall-Lerner condition if BoP is in *foreign* currency

$$CA^* = \frac{1}{S} P_{EX} q_{EX} - P_{IM}^* q_{IM} = \frac{1}{S} CA \qquad \eta_{EX} + \eta_{IM} \frac{SP_{IM}^* q_{IM}}{P_{EX} q_{EX}} > 1 \qquad \eta_{EX} + \eta_{IM} > 1$$

- elasticity empirical measurement and debate
  - elasticity optimism: sum is sufficiently high (>1) => Marshall-Lerner holds
  - elasticity *pessimism*: sum is too low (<1) => Marshall-Lerner *violated*
  - Hooper, Johnson and Marquez (2000): G-7, only for F and D found too low
- **equilibrium** in the *forex* market ≡ excess demand for *foreign exchange* (under PCP) is zero => *stability* analysis: Fig. 7.1, p. 90, in Gandolfo

 $ED_{fx}(S) \equiv D_{fx}(S) - S_{fx}(S) = P_{IM}^* IM(S) - \frac{1}{S} P_{EX} EX(S) = 0 \quad ED_{fx}(S) \ge 0 \iff CA \le 0$ 

- main **peculiarity** of demand/supply schedules for *foreign exchange* 
  - derived (indirect), i.e. induced by underlying demand schedules for *goods*: for domestic goods by *nonresidents* and for foreign goods by *residents*
  - consequence: even if underlying schedules for *goods* well-behaved, resulting schedules for *foreign exchange* may be abnormal => *multiple* equilibria

### Multiplier approach: assumptions

- introduced by **Harrod** (1933), before the Keynesian theory of the multiplier, to which it has many parallels
- another *flow* approach to BoP, whereby NER is assumed fixed, in addition to *prices* => suitable to analyse the adjustment process under a peg regime
- with *all* prices (including the exchange rate and the *interest rate*) constant, the only possibility for BoP adjustment in the model is by **changes in (national) income**
- underemployed resources
- all *exports* are made out of *current* output
- **absence of capital mobility**, so that the **BoP** is synonymous with the balance on goods and services or the current account (**CA**)

#### Multiplier approach: model set-up

• the *foreign trade multiplier model* is the *standard closed-economy Keynesian textbook model* with an **appended external sector** (the *linear* functions below are assumed for simplicity)

$$C = C_0 + C_1 Y, \qquad 0 < C_1 \equiv \frac{\partial C}{\partial Y} < 1$$
$$I = I_0 + I_1 Y, \qquad 0 < I_1 \equiv \frac{\partial I}{\partial Y} < 1$$
$$IM = IM_0 + IM_1 Y, \qquad 0 < IM_1 \equiv \frac{\partial IM}{\partial Y} < 1$$
$$EX = EX_0$$
$$Y \equiv C + I + EX - IM$$

 $\equiv CA \approx BoP$ 

• government expenditure (often denoted by *G* in similar set-ups) is not explicit in the above equation, but is considered as *present in the autonomous components* of the expenditure functions

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#### Multiplier approach: model solution

• **substituting** the four *expenditure functions* into *national income*:

$$Y = \frac{1}{1 - C_1 - I_1 + IM_1} (C_0 + I_0 - IM_0 + EX_0)$$
  
1 - C\_1 - I\_1 + IM\_1 > 0  $\Leftrightarrow \qquad \underbrace{C_1 + I_1 - IM_1}_{C_1 + I_1 - IM_1} < 1$ 

 $\equiv$  residents' marginal propensity to spend on *domestic* output

$$\Delta Y = \underbrace{\frac{1}{1 - C_1 - I_1 + IM_1}}_{(\Delta C_0 + \Delta I_0 - \Delta IM_0 + \Delta EX_0)}$$

 $\equiv$  open-economy multiplier

recall that the open-economy multiplier above is *smaller* than that for the *corresponding closed-economy* with the *same* 0 < C<sub>1</sub> < 1 and 0 < I<sub>1</sub> < 1 because of the additional leakage due to imports: the 0 < IM<sub>1</sub> < 1 term is *absent* in the respective closed-economy multiplier formula

Multiplier approach: BoP adjustment following an *exogenous* increase in **exports** 

$$\Delta CA = \Delta EX - \Delta IM = \Delta EX_0 - \underbrace{\Delta IM_0}_{=0} -IM_1 \Delta Y = \Delta EX_0 - IM_1 \Delta Y$$
$$\xrightarrow{=0} \Delta Y = \frac{1}{1 - C_1 - I_1 + IM_1} \Delta EX_0$$

$$\Delta CA = \Delta EX_0 - IM_1 \Delta Y = \Delta EX_0 - IM_1 \frac{1}{1 - C_1 - I_1 + IM_1} \Delta EX_0 =$$

$$= \left(1 - \frac{IM_1}{1 - C_1 - I_1 + IM_1}\right) \Delta E X_0 = \frac{1 - C_1 - I_1}{1 - C_1 - I_1 + IM_1} \Delta E X_0$$

- *complete* adjustment: *MPSpend*  $\equiv C_1 + I_1 = 1 => \Delta CA = 0$
- *under*adjustment: *MPSpend*  $\equiv C_1 + I_1 < 1 => \Delta CA < \Delta EX_0$
- *over*adjustment: *MPSpend*  $\equiv C_1 + I_1 > 1 => /\Delta CA / > \Delta EX_0$

# Multiplier approach: BoP adjustment following an *exogenous* increase in **imports** (I)

a *complication* arises, so one has to consider at least **two extremes** (and the possibility of *intermediate* cases)

- assume that the  $\uparrow$  in autonomous imports (i.e. in the exogenous expenditure by *residents* on *foreign* output),  $\Delta IM_0 \equiv \Delta C_{0F} + \Delta I_{0F} > 0$ is accompanied by a *simultaneous*  $\downarrow$  *in the same amount* in the exogenous expenditure by *residents* on *domestic* output,  $\Delta DA_0 \equiv \Delta C_{0H} + \Delta I_{0H} < 0$ so that  $\Delta C_0 + \Delta I_0 = (\Delta C_{0F} + \Delta I_{0F}) + (\Delta C_{0H} + \Delta I_{0H}) \equiv \Delta IM_0 + \Delta DA_0 = 0$
- assume that the exogenous  $\uparrow$  in imports is *not accompanied* by any  $\downarrow$  or  $\uparrow$  in exogenous expenditure on domestic output by residents, which remains *unchanged*, so that

 $\Delta C_0 + \Delta I_0 \equiv (\Delta C_{0H} + \Delta I_{0H}) + (\Delta C_{0F} + \Delta I_{0F}) = 0 + (\Delta C_{0F} + \Delta I_{0F}) \equiv \Delta I M_0$ 

in the latter case, with  $\Delta C_0 + \Delta I_0 = \Delta I M_0$  and  $\Delta E X_0 = 0$ 

it is seen from the multiplier formula that the numerator becomes 0, therefore *no adjustment is possible through induced changes in imports* and the *BoP deteriorates by the full amount of the exogenous*  $\uparrow$  *in imports*,  $\Delta CA = -\Delta IM_0$ 

# Multiplier approach: BoP adjustment following an *exogenous* increase in **imports** (II)

in the former case, implying *perfect substitutability* of the home and foreign good (a very *restrictive* assumption), *under*adjustment, *exact* adjustment and *over*adjustment will occur whenever  $C_1 + I_1 \leq 1$ , which becomes clear below

$$\Delta CA = \Delta EX - \Delta IM = \underbrace{\Delta EX_0}_{=0} -\Delta IM_0 - IM_1 \Delta Y = -\Delta IM_0 - IM_1 \Delta Y$$
$$\underbrace{\Delta Y}_{=0} \Delta Y = -\frac{1}{1 - C_1 - I_1 + IM_1} \Delta IM_0$$

$$\Delta CA = -\Delta IM_0 - IM_1 \Delta Y = -\Delta IM_0 + IM_1 \frac{1}{1 - C_1 - I_1 + IM_1} \Delta IM_0 =$$

$$= \left(-1 + \frac{IM_1}{1 - C_1 - I_1 + IM_1}\right) \Delta IM_0 = \frac{C_1 + I_1 - 1}{1 - C_1 - I_1 + IM_1} \Delta IM_0$$

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#### Multiplier approach: the transfer problem

- origins: war reparations on Germany after World War I
- **meaning:** understand effects, primary (immediate) and secondary (induced), of a (unilateral) **transfer of funds** from a *transferor* country to a *transferee* country on the BoP, that is, on the *current account* of the *transferor*
- **question:** will the BoP, understood as the CA (only), of transferor improve by a sufficient amount to "effect" the transfer
- **3 cases** possible:
  - 1. TB improves *less* than amount of transfer, CA *worsens*: *under*effected transfer
  - 2. TB improves *as much as* amount of transfer, CA is *same*: effected transfer
  - 3. TB improves *more* than amount of transfer, CA *improves*: *over*effected transfer
- early literature on transfer problem boils down to
  - Keynes (1929): transfer *under*effected, vs Ohlin (1929): transfer effected
  - conflicting outcome of findings results from the *different approaches* applied

## Transfer problem:

## Keynes (1929) and the classical theory

#### • assumptions

- 1. transferee, say *F*, disposes of transfer so as to reduce aggregate expenditure abroad, i.e. in transferor economy *H*, and increase aggregate expenditure domestically by *exact* amount of transfer
- 2. continuous *full* employment
- 3. external *equilibrium* before the transfer
- 4. entire income spent on purchases of goods
- **analysis**, for *H* (elements correspond to 3 terms in result below)
  - 1. initial deterioration by an amount equal to the transfer
  - 2. improvement due to lower expenditure, hence, lower imports
  - 3. improvement due to higher expenditure abroad, hence higher exports
- **result:**  $\Delta CA = -TR + IM_1TR + IM_1^*TR = (IM_1 + IM_1^* 1)TR$  **hence**  $IM_1 + IM_1^* \ge 1 \iff \Delta CA \ge 0$  but as "pessimism",  $IM_1 + IM_1^* < 1$ dominated, *under*effectuation was the conclusion, e.g. Keynes

### Transfer problem: Ohlin (1929) and the multiplier theory

- **assumptions:** differ from classical theory in 3 respects
  - *1. saving* allowed, so that  $\downarrow / \uparrow$  in expenditure may not relate one-to-one with amount of transfer in transfer-or/-ee country
  - 2. (Keynesian) situation of *underemployment*
  - 3. any exogenous change gives rise to further, **multiplier effects** on *income*, so that **induced changes** in *imports* have also to be considered when calculating overall effect on CA
- **analysis:** 1. transfer, 2. simultaneous changes in autonomous components, 3. multiplier effects, 4. induced changes  $\Delta C_0 = -C_{TR}TR$ ,  $\Delta C_0^* = C_{TR}^*TR$ (1., 2. and 4. correspond to terms in result  $\Delta I_0 = -I_{TR}TR$ ,  $\Delta I_0^* = I_{TR}^*TR$ below, 3. comes from multiplier)  $\Delta IM_0 = -IM_{TR}TR$ ,  $\Delta IM_0^* = IM_{TR}^*TR$
- result:  $\Delta CA = -TR + (\Delta IM_0^* \Delta IM_0) (IM_Y^* \Delta Y^* IM_Y \Delta Y)$ 
  - all three cases possible, and analysis much more complicated
  - most likely is, again, *under*effectuation
  - but Ohlin's opinion was of an effected transfer

#### An integrated approach to BoP adjustment: Laursen-Metzler (1950) model

- now **combine** the *elasticity* and *multiplier* approaches and consider a simpler, *SOE* version of original two-country model
  - denote by *Y* national *money* income and
    - assume *constant domestic* price level, *normalised* at 1: then
    - variations in *Y* measure variations in *physical* output (too)
  - *IM* and *EX* depend on
    - *ToT*, as in *elasticity* approach,
    - and -- assuming that price level *abroad* is *also constant* -- on *NER*: *EX* vary in *same* direction as *S*, and *IM* in *opposite* direction
  - IM also depend on *income Y*, as in *multiplier* approach
- NER, *S*, thus *coincides* with the relative price of imports, i.e. ToT
  - hence,  $\Delta S$  determines split-up of C and I b/n domestic and foreign goods
  - if appreciation ( $\downarrow$  in NER), imports become cheaper, so the *real* income corresponding to a *given money* income  $\uparrow$ , but as some of this  $\uparrow$  is **saved**, amount spent on goods will  $\downarrow$ : **Harberger-Laursen-Metzler effect**

#### Laursen-Metzler (1950): stability analysis

• in its simplified *SOE* version, model *reduces to* **two equations** Y = DA(Y,S) + CA

$$CA = 1 \cdot EX(S) - SP_{IM}^*IM(Y,S)$$

where the *domestic* price level has been normalised to 1

- model is **indeterminate**: 2 equations in 3 unknowns, (*Y*,*CA*,*S*)
- imposing **BoP equilibrium**, write 2nd equation as CA = 0 and
  - solve the resulting system for the remaining two unknowns, (Y,S),
  - which determines the *equilibrium point*  $(Y_e, S_e)$
- *diagrammatically*, the system can be represented as two curves in the (*Y*,*S*) plane: **stability analysis**, Fig. 9.3, p. 123, in Gandolfo
  - all points whose coordinates satisfy 1st equation determine the curve ensuring *real-market* equilibrium: RR curve
  - all points whose coordinates satisfy 2nd equation determine the curve ensuring *BoP* (*that is, CA*) equilibrium: BB curve
  - the intersection of the two curves yields the equilibrium (point) of model

#### The J-curve and the S-curve

- **transfer problem** in Laursen-Metzler model: if *stability* is to obtain (by suitable conditions on elasticities => slopes) transfer will always be *effected*
- **J-curve**: describes the *dynamics* of net exports (i.e. CA), with *time* on the horizontal axis, following a depreciation
- **S-curve**: indeed, a *horizontal* S resembling the *cross-correlation* structure (function) of net exports with ToT at short, medium and long lag/lead *horizon* (on the horizontal axis)
- Magee (1973): J-curve results from adjustment lags
  - *currency-contract* period: p and q fixed
  - *pass-through* period: p can be modified but not q, due to rigidities in demands for imports and exports
  - quantity-adjustment period: both p and q free to move

#### Does a float really insulate the economy?

- earlier research has led to the impression that flexible exchange rates *completely* insulate the domestic economy from the rest of the world, given that the suitable stability conditions are verified: Y=C+I+CA and since CA=0 under float, Y=C+I
- conclusion about the insulating properties of flexible exchange rates seems incorrect for (at least) 3 reasons
  - 1. adjustment following variations in NER is **not instantaneous**, i.e. it takes some time, therefore the *J-curve*
  - 2. NER variations have an effect
    - on *composition* of AD (b/n home and foreign good) inducing substitution
    - but also on the overall *level* of AD, affecting income: the essence of the Laursen-Metzler-Haberger effect
  - 3. the trade account (or the current account) needs not be balanced if *capital movements* are not abstracted away, which Laursen and Metzler (1950) did for the sake of simplicity

#### Mundell-Fleming (early 1960s) static model

- an extension to the *open* economy of Keynes (1936) Hicks (1937) IS-LM model
- assumptions
  - the *domestic* economy, *H(ome)*, is small, so that it takes foreign variables as given: SOE
  - *goods* prices are **fixed** (for the duration of the analysis)
  - but asset markets are continuously in equilibrium, due to full capital mobility

#### Mundell-Fleming model: derivation

• *open*-economy **IS** curve ⇔ *goods* market equilibrium

$$y = \delta(s + p^* - p) + \gamma y - \sigma \iota + g$$

• LM curve ⇔ *money* market equilibrium

$$m-p = \phi y - \lambda \iota$$

- FF curve ⇔ *international capital* market equilibrium, given by UIP with *static* expectations ι = ι\*
- substituting the domestic interest rate using UIP in IS and LM and then totally differentiating them (as shown in detail in the lecture notes), one obtains the following system of 2 equations

$$dy = \frac{\delta}{1-\gamma}ds - \frac{\sigma}{1-\gamma}dt^* + \frac{1}{1-\gamma}dg$$

$$dm = \frac{\phi\delta}{1-\gamma}ds - \left(\lambda + \frac{\phi\sigma}{1-\gamma}\right)d\iota^* + \frac{\phi}{1-\gamma}dg$$

#### Mundell-Fleming model: policy analysis

- all **comparative statics** results on the use of this model for *macroeconomic policy* analysis come from the above system
- *policy analysis* under **peg** => graphical interpretation
  - domestic credit expansion: Fig. 8.1 in Mark (2001)
  - domestic currency devaluation: Fig. 8.2 in Mark (2001)
  - expansionary fiscal policy: works in the same way as devaluation
  - foreign interest rate rise: Fig. 8.3 in Mark (2001)
  - implied international transmission
- *policy analysis* under **float** => graphical interpretation
  - domestic credit expansion: Fig. 8.4 in Mark (2001)
  - expansionary fiscal policy: Fig. 8.5 in Mark (2001)
  - foreign interest rate rise: Fig. 8.6 in Mark (2001)
  - implied international transmission

### Concluding wrap-up

#### • What have we learnt?

- distinguish b/n the elasticity and the multiplier approach to BoP adjustment (both **flow** approaches)
- derive and interpret the Marshall-Lerner condition
- describe and analyse the transfer problem
- summarise the Laursen-Metzler (1950) model, which **integrates** the elasticity approach with the multiplier approach, and discuss its stability
- derive and interpret the policy implications of the original, static Mundell-Fleming model, which is largely a flow approach, again, but already with some first elements of a stock approach to BoP
- Where we go next: to the richer, stock and stock-flow approaches to BoP adjustment